# Microeconomic Theory Review

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Vassar College

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# Evaluate the Earned Income Tax Credit (EITC)

- For 2025, the NY EITC will rise from 30% to 45% of the federal EITC
- Gov. Hochul asks how this will affect hours worked and labor force participation
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- What can you say with near certainty?
- What are you less certain about?
- Depends on (1) the shape of the EITC and (2) your model of behavior

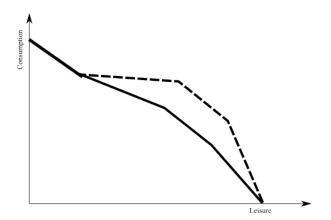


Figure 1: The EITC budget constraint where "leisure" is time not spent working. As "leisure" rises, labor supply falls.

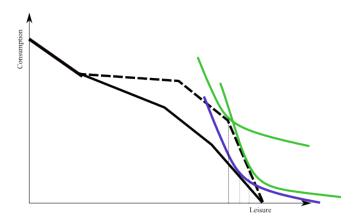


Figure 2: On the "phase-in," substitution reduces leisure, but income effect positive.

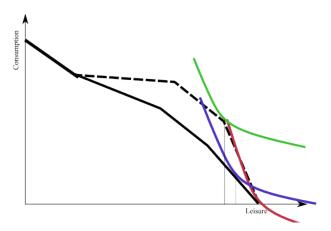


Figure 3: But no one stops working who is working.

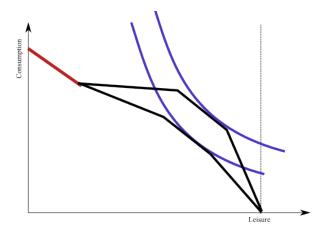


Figure 4: Someone on the "flat" of the EITC just receives an income effect. If we assume leisure is a "normal" good, then that means more leisure, less working.

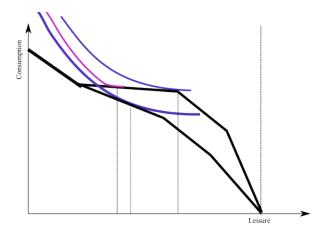


Figure 5: Someone on the "phase-out" of the EITC gets an income and substitution effect towards more leisure. If leisure is a normal good, the purple line is impossible.

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#### Empirical analysis

- Use data to estimate relationships between variables
- Can be used to test theories
- Often all about causal inference

### **Economic Theory Tools**

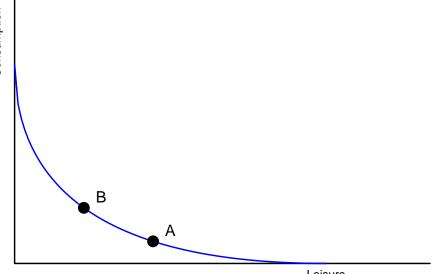
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- Indifference curves



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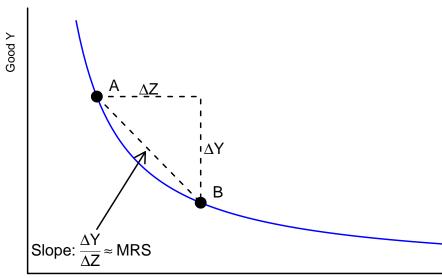
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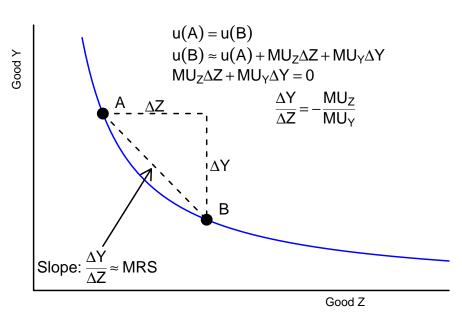
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$$MRS = -\frac{MU_Z}{MU_Y} = -\frac{10/Z}{20/Y} = -\frac{1}{2}\frac{Y}{Z}$$







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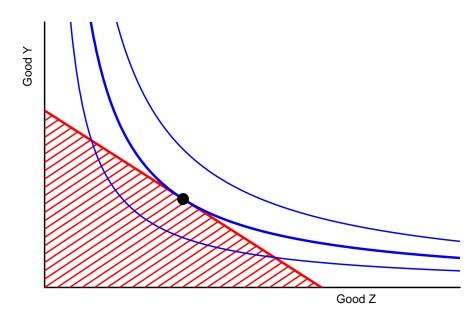
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 $P_Y = 10, P_Z = 20, Y = 120$   
Submit an answer

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Solution: Z = Y = 4.



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 $\Rightarrow$  hence  $Z = 4$  and  $Y = 12-2Z = 4$ .

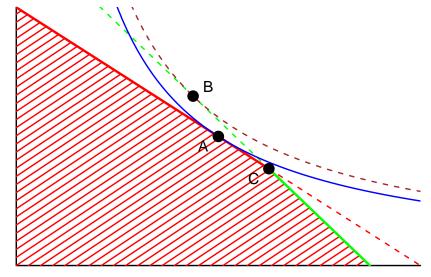


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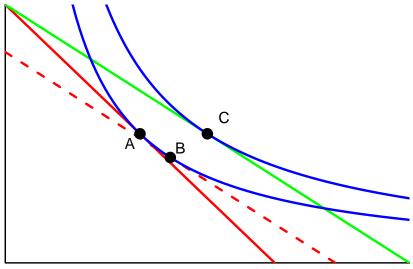
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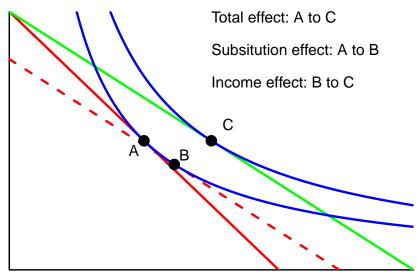
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- Examples:
  - Earned Income Tax Credit (we'll talk more about it) provides a marginal subsidy if earnings are not too large and then slowly takes it away. Many related provisions in welfare programs.
  - Tax exemptions no tax (labor valuable, leisure costly) up to certain income level, tax afterwards.
  - Progressive taxation price of labor depends on your income.
  - Health insurance subsidies the amount depends on the level of income.



## Income and substitution effects



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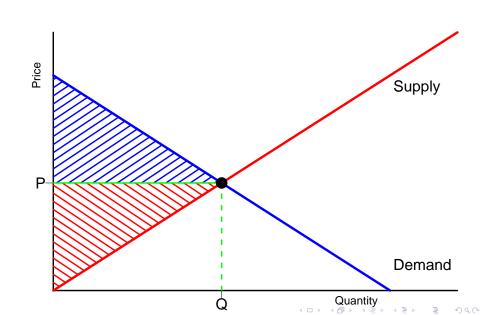
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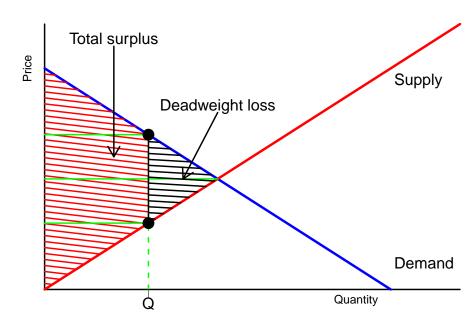
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• You can see it by substituting  $x = \ln(p)$  so that  $\frac{d \ln(D(p))}{d \ln(p)} = \frac{d \ln(D(e^{\ln(x)}))}{dx}$  and work through the derivative with respect to x.

# Equilibrium and efficiency





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## Edgeworth Box

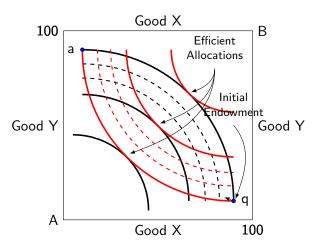


Figure 6: Edgeworth Box shows where marginal rates of substitution equate.

### Contract curve: All Pareto efficient allocations

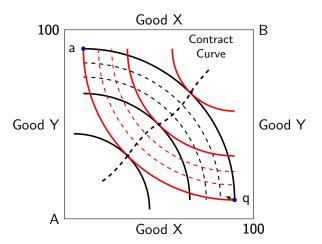


Figure 6: Contract curve: Locus of Pareto efficient allocations.

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- Anyone have guesses at a potential problem?

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# Illustrating 2nd Welfare Theorem fallacy

Suppose 50% of the economy is unable to work due to disability (earn \$0) and 50% can work, earn \$100

Free market outcome: disabled get \$0, able-bodied get \$100

2WT: gov't differentiates disabled and able-bodied perfectly

 $\Rightarrow$  taxes the able-bodied \$50 and gives to each disabled person

Instead: gov't can't tell apart disabled/able-bodied, uses work status

- $\Rightarrow$  \$50 tax on workers + \$50 transfer to non-workers  $\downarrow$  incentive to work
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⇒ 2WT is a useful benchmark, but poor practical policy prescription



### Summary

- We rely on basic microeconomic tools: utility to represent preferences, budget constraints, utility maximization, demand, supply, equilibrium
- Important concepts: marginal rate of substitution, income and substitution effects, elasticity, Pareto efficiency, deadweight loss
- Welfare theorems:
  - 1st: reference point, we will talk about deviations from it (market failures)
  - 2nd: focus on fairness but unrealistic method of redistribution